

M.M. =75

Time: 3 hrs

Note: Candidates are required to attempt **Five** questions in all by selecting at least **Two** questions each from the section A and B. Section C is compulsory. *Non - Prog. Scientific Calculator is allowed.*

Section-A

Q1: (a) If A and B have n elements in common. Show that $A \times B$ and $B \times A$ have n^2 elements in common.

(b) How many subsets can be formed from a set of n elements? How many of these will be proper and how many improper?

Q2: (a) Test the validity: Either I will get good marks or I will not graduate. If I did not graduate I will go to Australia. I get good marks. Thus, I would not go to Australia.

(b) Find the domain, range and inverse of the relation given by R:

$$\{(x, y): y = x + \frac{10}{x}, \text{ where } x, y \in N \text{ and } x < 10\}.$$

Q3: Prove by the principle of induction: $x^n - y^n$ is divisible by $x - y$.

Q4: (a) Let R be the relation on the set $\{0,1,2,3\}$ containing the ordered pairs (0,1), (1,1), (1,2), (2,0), (2,2), and (3,0). What is the reflexive closure, symmetric closure and transitive closure of R?

(b) Partition $A = \{1,2,3,4,5,6,7\}$ with the minsets generated by $B_1 = \{2,4,6\}$ and $B_2 = \{1,4,5\}$ and also find out how many different subsets of A can you generate from B_1 and B_2 ?

Section-B

Q5: (a) Explain in detail the representation of the directed graphs and also give one example.

(b) Define Planner graph and regions. State and prove the properties for a graph to be planner graph.

Q6: (a) Define function and explain different types of functions.

(b) If $f: A \rightarrow B$ and $g: B \rightarrow C$ are two bijections, then show that $(f \circ g)^{-1} = g^{-1} \circ f^{-1}$.

Q7: (a) Define Complete Bipartite graph and give example. Find the number of edges if the graph G has 5 vertices, 2 of degree 3 and 3 of degree 2.

(b) An Undirected graph possesses an Eulerian path iff it is connected and has either zero or two vertices of odd degree.

Q8: (a) Prove that in a complete graph the number of edges is $\frac{n(n-1)}{2}$. How many vertices are there in a graph with 10 edges if each vertex has degree 2?

(b) Let G be a finite graph with $n > 1$ vertices. Prove that G is tree iff it is minimally connected.

Section-C

Q9: (i) Define ordered pair and Cartesian product? (3)

- (ii) Define union of two sets and give one example of each. (3)
- (iii) Define totally ordered relation and give an example. (1)
- (iv) Define Big-Theta Notation. (1)
- (v) Define Ceiling function. (1)
- (vi) Explain the travelling salesman problem. (3)
- (vii) Explain the Kruskal's Algorithm for minimum spanning tree. (3)

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